Introduction to Sage

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Mission Statement

Create a viable **free open source** alternative to Magma, Maple, Mathematica, and Matlab

- Mathematical features of all of Magma, Maple, Mathematica, and Matlab
- A notebook interface
- Many books (undergraduate/grad curriculum)



Sage Timeline

- **2005:** I released Sage 0.1... long year of very hard work.
- 2006: (2 Sage Days) Sage is not just for number theory!
- 2007: (4 Sage Days) Win prize—tons of publicity; 100% test requirements and peer review of all code; industry funding (Google, Microsoft).
- 2008: (7 Sage Days) Release managers besides me.
- **2009:** (8 Sage Days) Better quality; more developers.
- **2010:** (13 Sage Days) More people; serious NSF support.
- 2011: Revamping web interface (due to new funding), undergrad curriculum materials, new research tools.



What is Sage?

Sage

- Python: a mainstream programming language
- Distribution: over 90 open source packages
- Interfaces: smoothly combine packages
- New code: implements novel algorithms; over half million lines written by several hundred people.





47,942 Website Visits this month (Feb 2011)



Sage has interest from all over, but is still relatively small... (No advertising yet; all word of mouth/grassroots.)

The Sage Notebook

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SCAP The Sage Notebook	

Welcome!

Version 4.6

Sage is a different approach to mathematics software.

The Sage Notebook

With the Sage Notebook anyone can create, collaborate on, and publish interactive worksheets. In a worksheet, one can write code using Sage, Python, and other software included in Sage.

General and Advanced Pure and Applied Mathematics

Use Sage for studying calculus, elementary to very advanced number theory, cryptography, commutative algebra, group theory, graph theory, numerical and exact linear algebra, and more.

Use an Open Source Alternative

By using Sage you help to support a viable open source alternative to Magma, Maple, Mathematica, and MATLAB. Sage includes many high-quality open source math packages.



MAA talk on Sage - 20min

MAA Talk on Sage

William Stein

February 26, 2011, Santa Rosa

Factor

Factoring an integer:

factor(2012)

 $2^2 \cdot 503$

Factoring a symbolic expression:

var('x,y')
factor(x^8 - y^2*e^(2*x))

 $(x^4 - ye^x)(x^4 + ye^x)$

Graph Theory

set_random_seed(1); G = graphs.RandomLobster(7, .6, .3); show(G)



True			

Symbolic Integrals

 $\begin{array}{l} \\ & \text{integrate(sin(x) * tan(x), x)} \\ & -\frac{1}{2} \log \left(\sin \left(x \right) - 1 \right) + \frac{1}{2} \log \left(\sin \left(x \right) + 1 \right) - \sin \left(x \right) \\ & \text{f} = 1/\operatorname{sgrt}(x^2 + 2^*x - 1) \\ & \text{f.integrate(x)} \end{array}$

 $\log \left(2x + 2\sqrt{x^2 + 2x - 1} + 2\right)$

Plotting Functions

plot(sin(x^2), (x,0,5))





Plotting a Function in 3D

```
 \begin{array}{l} f(x,y) = \sin(x-y)*y*\cos(x) \\ plot3d(f, (x,-3,3), (y,-3,3), opacity=.7, color='red') + \\ icosahedron(color='blue') \end{array}
```



An implicit 3D plot:

T = RDF(golden_ratio) var('x,y,z') p = (2 - (cos(x + T*y) + cos(x - T*y) + cos(y + T*z) + cos(y - T*z) + cos(z - T*x) + cos(z + T*x))) r = 4.77 implicit_plot3d(p, (x, -r, r), (y, -r, r), (z, -r, r), plot points=40)



Image Compression

```
import pylab; import numpy
A_image = numpy.mean(pylab.imread(DATA + 'santarosa.png'), 2)
u,s,v = numpy.linalg.svd(A_image); S = numpy.zeros( A_image.shape)
S[:len(s),:len(s)] = numpy.diag(s)
n = A_image.shape[0]
&interact
def svd_image(i = ("Eigenvalues (quality)",(20,
(1..A_image.shape[0]/(2)))):
A_approx = numpy.dot(numpy.dot(u[:,:i], S[:i,:i]), v[:i,:])
g = graphics_array((matrix_plot(A_approx),
matrix_plot(A_image)])
show(g, axes=False, figsize=(10,6))
```


Eigenvalues (quality) 20

Compressed to 14.1% of size using 20 eigenvalues.





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